



Design of Oil-Lubricated Machine Components for Life and Reliability

Erwin V. Zaretsky
Glenn Research Center, Cleveland, Ohio

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Prepared for the
Seventh International Symposia on Tribology (INSYCONT 2006)
cosponsored by the AGH University of Science and Technology, the Polish Academy of Science,
the Institute for Terotechnology, and the Polish Tribology Society
Cracow, Poland, September 14–16, 2006

National Aeronautics and
Space Administration

Glenn Research Center
Cleveland, Ohio 44135

This work was sponsored by the Fundamental Aeronautics Program
at the NASA Glenn Research Center.

Level of Review: This material has been technically reviewed by technical management.

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Summary

In the post-World War II era, the major technology drivers for improving the life, reliability, and performance of rolling-element bearings and gears have been the jet engine and the helicopter. By the late 1950s, most of the materials used for bearings and gears in the aerospace industry had been introduced into use. By the early 1960s, the life of most steels was increased over that experienced in the early 1940s, primarily by the introduction of vacuum degassing and vacuum melting processes in the late 1950s. The development of elastohydrodynamic (EHD) theory showed that most rolling bearings and gears have a thin film separating the contacting bodies during motion and it is that film which affects their lives. Computer programs modeling bearing and gear dynamics that incorporate probabilistic life prediction methods and EHD theory enable optimization of rotating machinery based on life and reliability. With improved manufacturing and processing, the potential improvement in bearing and gear life can be as much as 80 times that attainable in the early 1950s. The work presented summarizes the use of laboratory fatigue data for bearings and gears coupled with probabilistic life prediction and EHD theories to predict the life and reliability of a commercial turboprop gearbox. The resulting predictions are compared with field data.

Introduction

By the close of the 19th century, the bearing industry began to focus on sizing bearings for specific applications and determining bearing life and reliability. In 1896, R. Stribeck (ref. 1) in Germany began fatigue testing full-scale bearings. J. Goodman (ref. 2) in 1912 in Great Britain published formulas based on fatigue data that would compute safe loads on ball and cylindrical roller bearings. In 1914, the "American Machinists Handbook and Dictionary of Shop Terms" (ref. 3) devoted six pages to rolling-element bearings, discussing bearing sizes and dimensions and recommending (maximum) loading and specified speeds. However, this publication did not address the issue of bearing life. During this time, it would appear that rolling-element bearing fatigue testing was the only way to determine or predict the minimum or average life of ball and roller bearings.

In 1924, A. Palmgren (ref. 4) in Sweden published a paper in German outlining his approach to bearing life prediction and presented an empirical formula based upon the concept of an L_{10} life, or life at which 90 percent of a population survives.

During the next 20 years, he empirically refined his approach to bearing life prediction and matched his predictions to test data (ref. 5). However, his formula lacked a theoretical basis or an analytical proof.

In 1939, W. Weibull (refs. 6 and 7) in Sweden published his theory of failure. He was a contemporary of Palmgren and shared the results of his work with him. In 1947, Palmgren in concert with G. Lundberg, also of Sweden, incorporated his previous work along with that of Weibull and what appears to be the work of H. Thomas and V. Hoersch (ref. 8) in a probabilistic analysis to calculate rolling-element (ball and roller) life. This has become known as the Lundberg-Palmgren theory (refs. 9 and 10). (In 1930, H. Thomas and V. Hoersch (ref. 8) at the University of Illinois, Urbana, developed an analysis for determining subsurface principal stresses under Hertzian contact (ref. 11). Lundberg and Palmgren (refs. 9 and 10) do not reference the work of Thomas and Hoersch (ref. 8) in their papers.)

The Lundberg and Palmgren life equations have been incorporated in both the International Organization for Standardization (ISO) and the American National Standards Institute (ANSI)/American Bearing Manufacturers Association (ABMA) standards for the load ratings and life of rolling-element bearings (refs. 12 to 14) as well as in current bearing codes to predict life.

In the post-World War II era, the major technology drivers for improving the life, reliability, and performance of rolling-element bearings and gears have been the jet engine and the helicopter. By the late 1950s, most of the materials used for bearings and gears in the aerospace industry were introduced into use. By the early 1960s, the life of most steels was increased over that experienced in the early 1940s, primarily by the introduction of vacuum degassing and vacuum melting processes in the late 1950s (ref. 15).

The development of elastohydrodynamic (EHD) lubrication theory in 1939 by A. Ertel (ref. 16) and later by A. Grubin (ref. 17) in 1949 showed that most rolling bearings and gears have a thin EHD film separating the contacting components. The life of these bearing and gears is a function of the thickness of the EHD film (ref. 15).

Computer programs modeling bearing and gear dynamics that incorporate probabilistic life prediction methods and EHD theory enable the optimization of rotating machinery based on life and reliability. With improved manufacturing and material processing, the potential improvement in bearing and gear life can be as much as 80 times that attainable in the early 1950s (ref. 15).

Between 1975 and 1981, Coy, Townsend, and Zaretsky (refs. 18 to 21) published a series of papers developing a methodology for calculating the life of spur and helical gears based upon the Lundberg-Palmgren theory and methodology for rolling-element bearings.

A probabilistic life model for planetary gear trains has been developed (refs. 22 to 27). This model is based on the individual reliabilities of the gearbox bearing and gears based on classical rolling-element fatigue. The reliability of the gearbox system is treated as a strict series probability combination of the reliabilities of the gearbox components based on the Lundberg-Palmgren theory (refs. 9 and 10). Each bearing and gear life was calculated and the results were statistically combined to produce a system life for the total gearbox. The method was applied to a turboprop gearbox by Lewicki, et al. (ref. 28).

The work presented in this report summarizes the use of laboratory fatigue data for bearings and gears coupled with probabilistic life prediction and EHD theories to (1) predict the life and reliability of a commercial turboprop gearbox and (2) compare the resulting prediction with field data.

Symbols

a	major semiaxis of contact ellipse, m (in.)
a_1	life adjustment factor for reliability
a_2	life adjustment factor for materials and processing
a_3	life adjustment factor for operating conditions including lubrication
B	gear material constant, $\text{N/m}^{1.979} (\text{lbf/in.}^{1.979})$
C_D	basic dynamic capacity of a ball or roller bearing, N (lbf)
C_t	basic dynamic capacity of gear tooth, N (lbf)
c	stress-life exponent
d	diameter of rolling element, m (in.)
e	Weibull slope; exponent
F_t	normal tooth load, N (lbf)
f	tooth face width, m (in.)
f_{cm}	bearing geometry and material coefficient

h	elastohydrodynamic (EHD) lubricant film thickness, m (in.); exponent
i	number of rows of rolling elements
k	gear tooth stress cycles per input shaft revolutions
L	life, hr, stress cycles, or revolutions
L_β	characteristic life or life at which 63.2 percent of population fails, hr, stress cycles, or revolutions
L_{10}	10-percent life or life at which 90 percent of a population survives, hr, stress cycles, or revolutions
l	length of stressed track, m (in.)
ℓ	roller length, m (in.)
N	number of gear teeth
n	life, stress cycles
P_{eq}	equivalent bearing load, m (in.)
p	load-life exponent
r	pitch circle radius of gear, m (in.)
S	probability of survival, fractional percent
V	stressed volume, m^3
X_n	fraction of time spent at load-speed condition n
Z	number of rolling elements per row
z	depth beneath the surface of maximum orthogonal or maximum shear stress, m (in.)
α	contact angle, deg
η_{10t}	L_{10} life of single gear tooth, stress cycles
Λ	lubrication film parameter h/σ (eq. (14))
ρ	curvature sum, $\text{m}^{-1} (\text{in.}^{-1})$
σ	composite surface roughness, rms, m (in.)

σ_1, σ_2	surface roughness of bodies 1 and 2, rms, m (in.)
τ	maximum orthogonal or maximum shear stress, Pa (psi)
ϕ	gear pressure angle, deg

Subscripts

1, 2	bodies 1 or 2; load-life condition 1, 2, etc.
<i>B</i>	bearing
<i>G</i>	gear
<i>n</i>	body <i>n</i> or load-life condition <i>n</i>
<i>ref</i>	define
<i>s, sys</i>	system
<i>t</i>	tooth

Enabling Equations and Analysis

Weibull Analysis

In 1939, Weibull (refs. 6 and 7) developed a method and equation for statistically evaluating the fracture strength of materials. He also applied the method and equation to fatigue data based upon small sample (population) sizes, where the two-parameter expression relating life and probability of survival is

$$\ln \ln \left(\frac{1}{S} \right) = e \ln \left(\frac{L}{L_\beta} \right) \quad \text{where } 0 < L < \infty; 0 < S < 1 \quad (1)$$

When plotting the $\ln \ln [1/S]$ as the ordinate against the $\ln L$ as the abscissa, fatigue data are assumed to plot as a straight line (fig. 1). The ordinate $\ln \ln [1/S]$ is graduated in statistical percent of components failed or removed for cause as a function of $\ln L$, the log of the time or cycles to failure. The tangent of the line is designated the Weibull slope e , which is indicative of the shape of the cumulative distribution or the amount of scatter of the data.

The method of using the Weibull distribution function for data analysis for determining component life and reliability was later developed and refined by Johnson (ref. 29). This method was used to analyze the data reported herein.

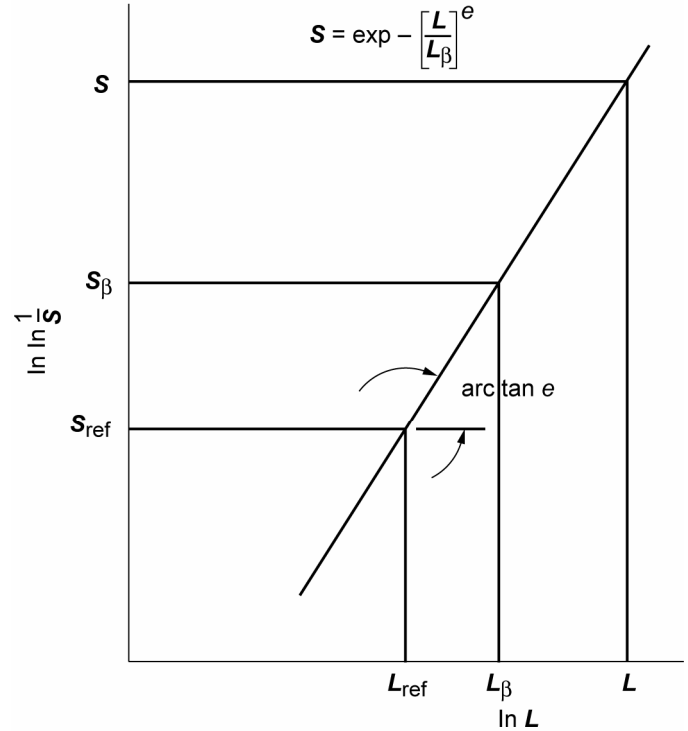


Figure 1.—Weibull plot where (Weibull) slope of tangent or line is e . Probability of survival S_β of 36.8 percent at which $L = L_\beta$ or $L/L_\beta = 1$.

Bearing Life Analysis

Lundberg and Palmgren (refs. 9 and 10) extended the theoretical work of Weibull (refs. 6 and 7) and showed that the probability of survival S could be expressed as a power function of shear stress τ , life n , depth of maximum shear stress z , and stressed volume V :

$$\ln \frac{1}{S} \sim \frac{\tau^c n^e}{z^h} V \quad (2)$$

$$\ln \frac{1}{S} \sim \frac{\tau^c n^e a l}{z^{h-1}} \quad (3)$$

By substituting the bearing geometry and the Hertzian contact stresses for a given load into equation (3), the bearing basic dynamic load capacity C_D can be calculated (ref. 9). The basic dynamic load capacity C_D is defined as the load that a bearing can carry for a life of one-million inner-race revolutions with a 90-percent probability of survival (L_{10} life). Lundberg and Palmgren (ref. 9) obtained the following additional relation:

$$L_{10} = \left(\frac{C_D}{P_{eq}} \right)^p \quad (4)$$

where P_{eq} is the equivalent bearing load and p is the load-life exponent.

Formulas for the basic dynamic load ratings derived by Lundberg and Palmgren (refs. 9 and 10) and incorporated in the ANSI/AFBMA and ISO standards (refs. 12 to 14) are as follows:

Radial ball bearings with $d \leq 25$ mm:

$$C_D = f_{cm} (i \cos \alpha)^{0.7} Z^{2/3} d^{1.8} \quad (5)$$

Radial ball bearings >25 mm:

$$C_D = f_{cm} (i \cos \alpha)^{0.7} Z^{2/3} d^{1.4} \quad (6)$$

Radial roller bearings:

$$C_D = f_{cm} (i \ell \cos \alpha)^{7/9} Z^{3/4} d^{29/27} \quad (7)$$

Equation (4) can be modified using life factors based on reliability a_1 , materials and processing a_2 , and operating conditions such as lubrication a_3 (refs. 15 and 30) where

$$L = a_1 a_2 a_3 L_{10} \quad (8)$$

Table 1 contains a list of representative variables that affect bearing life (ref. 30).

TABLE 1.—REPRESENTATIVE VARIABLES
AFFECTING BEARING LIFE AND RELIABILITY
[From ref. 30]

Life adjustment factor	Variable
Reliability, a_1	Probability of failure
Materials and processing, a_2	Bearing steel Material hardness Residual stress Melting process Metal working
Operating conditions, a_3	Load Misalignment Housing clearance Axially loaded cylindrical bearings Rotordynamics Hoop stresses Speed Temperature Steel Lubrication Lubricant film thickness Surface finish Water Oil Filtration

Gear Life Analysis

Between 1975 and 1981, Coy, Townsend, and Zaretsky (refs. 18 to 21) published a series of papers developing a methodology for calculating the life of spur and helical gears based upon the Lundberg-Palmgren theory and methodology for rolling-element bearings. Townsend, Coy, and Zaretsky (ref. 31) reported that for AISI 9310 spur gears, the Weibull slope e is 2.5. Based on equation (2), for all gears except a planet gear, the gear life can be written as

$$L_{10G} = \frac{N^{-1/e_G} \eta_{10t}}{k} \quad (9)$$

For a planet gear, the life is

$$L_{10G} = \frac{N^{-1/e_G} (\eta_{10t1}^{-e_G} + \eta_{10t2}^{-e_G})^{-1/e_G}}{k} \quad (10)$$

The L_{10} life of a single gear tooth can be written as

$$\eta_{10t} = a_2 a_3 \left(\frac{C_t}{F_t} \right)^{p_G} \quad (11)$$

where

$$C_t = B f^{0.907} \rho^{-1.165} l^{-0.093} \quad (12)$$

and

$$\rho = \left(\frac{1}{r_1} + \frac{1}{r_2} \right) \frac{1}{\sin \phi} \quad (13)$$

and η_{10t} is the L_{10} life in millions of stress cycles for one particular gear tooth. This number can be determined by using equation (11), where C_t is the basic load capacity of the gear tooth; F_t is the normal tooth load; p_G is the load-life exponent usually taken as 4.3 for gears based on experimental data for AISI 9310 steel; and a_2 and a_3 are life adjustment factors similar to that for rolling-element bearings (table 1). The value for C_t can be determined by using equation (12), where B is a material constant that is based on experimental data and is approximately equal to 1.39×10^8 when calculating C_t in SI units (newtons and meters) and 21 800 in English units (pounds and inches) for AISI 9310 steel spur gears; f is the tooth width; and ρ is the curvature sum at the start of single-tooth contact.

Life factors a_2 for materials and processing are determined experimentally. Table 2 shows representative life factors obtained from surface fatigue testing of spur gears by NASA (refs. 15 and 30).

TABLE 2.—RELATIVE SURFACE PITTING
FATIGUE LIFE FOR VAR AISI 9310 STEEL
AND AIRCRAFT-QUALITY GEAR STEEL
(ROCKWELL C 59 to 62)
[From refs. 15 and 30]

Steel ^a	10-percent relative life, L_{10}
VAR AISI 9310	1.0
VAR AISI 9310 (shot peened)	1.6
VIM-VAR AISI 9310	2.5
VAR Carpenter EX-53	2.1
CEVM CBS 600	1.4
VAR CBS 1000	2.1
CEVM Vasco X-2	2.0
CEVM Super Nitralloy (5Ni-2Al)	1.3
VIM-VAR AISI M-50 (forged)	3.2
VIM-VAR AISI M-50 (ausformed)	2.4
VIM-VAR M50 NiL	11.5

^aVAR, vacuum arc remelting; CEVM, consumable-electrode vacuum remelting; VIM-VAR, vacuum induction melting—vacuum arc remelting.

The L_{10_G} life of the gear (all teeth) in millions of input shaft revolutions at which 90 percent will survive can be determined from equation (9) or (10) where N is the total number of teeth on the gear; e_G is the Weibull slope for the gear and is assumed to be 2.5 (from ref. 31); and k is the number of load (stress) cycles on a gear tooth per input shaft revolution.

For all gears except the planet gears, each tooth will see load on only one side of its face for a given direction of input shaft rotation. However, each tooth on a planet gear will see contact on both sides of its face for a given direction of input shaft rotation. One side of its face will contact a tooth on the sun gear, and the other side of its face will contact a tooth on the ring gear. Equation (10) takes this into account, where $\eta_{10,1}$ is the L_{10} life in millions of stress cycles of a planet tooth meshing with the sun gear, and $\eta_{10,2}$ is the L_{10} life in millions of stress cycles of a planet tooth meshing with the ring gear.

Elastohydrodynamic Lubrication

An important parameter to consider when designing and operating rolling bearings and gears is the elastohydrodynamic (EHD) lubricant film thickness that forms between heavily loaded contacting bodies. Ertel (ref. 16) and Grubin (ref. 17) are credited with the first useful solution. A summary of EHD film thickness calculations can be found in reference 15.

The life of a rolling bearing or gear is a function of a lubrication film parameter Λ where

$$\Lambda = \frac{h}{\sigma} \quad (14)$$

and

$$\sigma = (\sigma_1^2 + \sigma_2^2)^{1/2} \quad (15)$$

The lubricant film parameter Λ can be used as an indicator of bearing and gear performance and life. For $\Lambda < 1$, surface smearing or deformation accompanied by wear will occur on the rolling surfaces. For $1 < \Lambda < 1.5$, surface distress may be accompanied by superficial surface pitting. For $1.5 < \Lambda < 3$, some surface glazing can occur with eventual failure caused by classical subsurface-origin, rolling-element fatigue. At $\Lambda \geq 3$, minimal wear can be expected with extremely long life, and failure will eventually be by classical subsurface-origin, rolling-element fatigue.

The most expedient way of attaining a higher Λ ratio is to reduce the bearing or gear operating temperature and thus increase the lubricant viscosity. Another way is to select a lubricant with a higher viscosity at operating temperature, a larger pressure-viscosity coefficient, or both. The most expensive way of attaining a higher Λ ratio is to select a high-quality surface finish on bearings and gears (refs. 15 and 30).

The effect of film thickness on bearing life is shown in figure 2. The life factor (LF) obtained from this figure is used to modify or adjust the calculated lives of bearings and gears (refs. 15 and 30). This constitutes the life factor a_3 in equations (8) and (11).

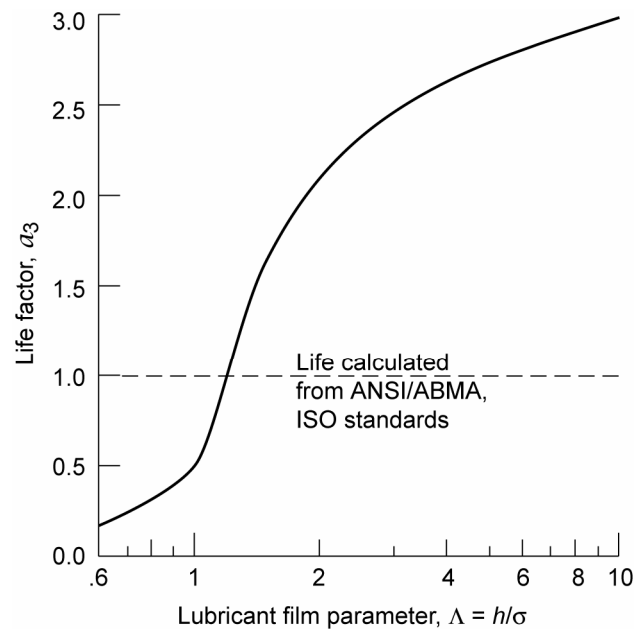


Figure 2.—Life factor a_3 as function of lubricant film parameter Λ (ref. 15).

System Life Prediction

The L_{10} lives of the individual bearings and gears that make up a rotating machine are calculated for each condition of their operating profiles. For each component, the resulting lives from each of the operating conditions are combined using the linear damage (Palmgren-Langer-Miner) rule (refs. 4, 32, and 33) where

$$\frac{1}{L} = \frac{X_1}{L_1} + \frac{X_2}{L_2} + \dots + \frac{X_n}{L_n} \quad (16)$$

The cumulative lives of each of the machine components are combined to determine the calculated machine system L_{10} life using the Lundberg-Palmgren formula (ref. 9):

$$\frac{1}{L_{sys}^e} = \left(\frac{1}{L_{B_1}^{e_B}} + \frac{1}{L_{B_2}^{e_B}} + \dots + \frac{1}{L_{B_n}^{e_B}} \right) + \left(\frac{1}{L_{G_1}^{e_G}} + \frac{1}{L_{G_2}^{e_G}} + \dots + \frac{1}{L_{G_n}^{e_G}} \right) \quad (17)$$

The calculated system life is dependent on the resultant value of the system Weibull slope e . This value is normally not known with absolute certainty and is usually assumed to be the same as that of the lowest lived component in the system.

Results and Discussion

Predicted Life of Turboprop Gearbox

A commercial turboprop gearbox used for this analysis is shown in figure 3. It consists of two stages with a single-mesh spur reduction followed by a 5-planet planetary gearbox comprising 11 rolling-element bearings and 9 spur gears (ref. 28). The first stage consists of the input pinion gear meshing with the main drive gear. The second stage is provided by the fixed-ring planetary driven by a floating sun gear as input with a five-planet carrier as output. The input pinion speed is constant at 13 820 rpm, producing a carrier output speed of 1021 rpm.

The operational profile includes loads for takeoff, climb, cruise, and descent. The cruise segment of the profile consumes 68 percent of the flight time with a little less than half of the power required for the takeoff, which lasts for less than 3 percent of the flight time.

The cause for removal can be assumed to be that one or more bearings or gears had fatigue or damage resulting in wear and/or vibration detected by magnetic chip detectors and/or vibration pickups. The gearboxes are removed from service before secondary damage occurs. The removed gearbox is inspected and the failed part or parts are replaced. The gearbox is then put back into service.

Individual occurrences are not predictable but are probabilistic. No two gearboxes run under the same conditions fail necessarily from the same cause and/or at the same time.

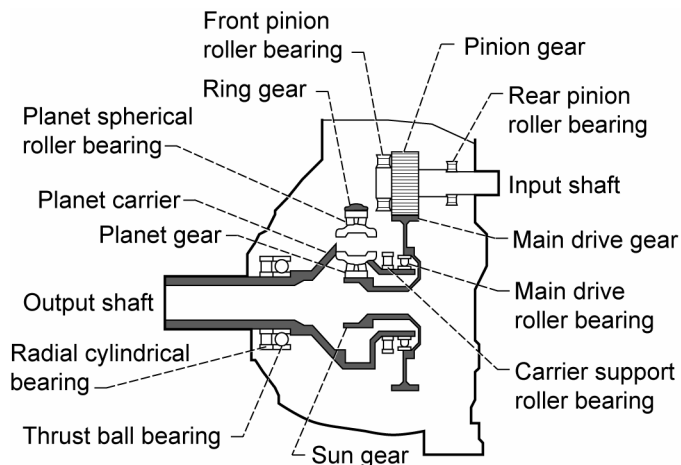


Figure 3.—Commercial turboprop gearbox.

At a given probability of survival, the life of the gearbox will always be less than the lowest lived element in the gearbox.

Using equations (4) through (8) for bearings and equations (9) through (13) for gears and appropriate computer programs incorporating these equations, the lives of each of the bearings and gears making up the gearbox were calculated for each of their operating conditions. These lives are shown as the Weibull plots in figure 4.

The L_{10} life of a single double-row spherical bearing is 3529 hr. From equation (14), the system L_{10} life for the five-bearing planetary set is 774 hr. For all the bearings in the gearbox, the bearing system L_{10} life is also predicted to be 774 hr.

Using equation (17) for the individual gears, the gear system predicted L_{10} life is 16 680 hr. Combining the bearing and gear lives to obtain a gearbox L_{10} life, again using equation (17), the predicted L_{10} life for the gearbox is 774 hr. The lives of the individual bearings, and more specifically, those of the planet double-row spherical bearings, determine the life of the gearbox in this example. The system lives of the bearings, gears, and gearbox are summarized in figure 4(c).

Gearbox Field Data

The application of the Lundberg-Palmgren theory (ref. 9) to predict gearbox life and reliability needs to be benchmarked and verified under a varied load and operating profile. The cost and time to laboratory test a statistically significant number of gearboxes to determine their life and reliability is prohibitive. A practical solution to this problem is to benchmark the analysis to field data. Fortunately, these data were available for the commercial turboprop gearbox used in this study.

No two gearboxes are expected to operate in exactly the same manner. Flight variables include operating temperature and load. Small variations in operational load can result in significant changes in life. Hence, the accuracy of our

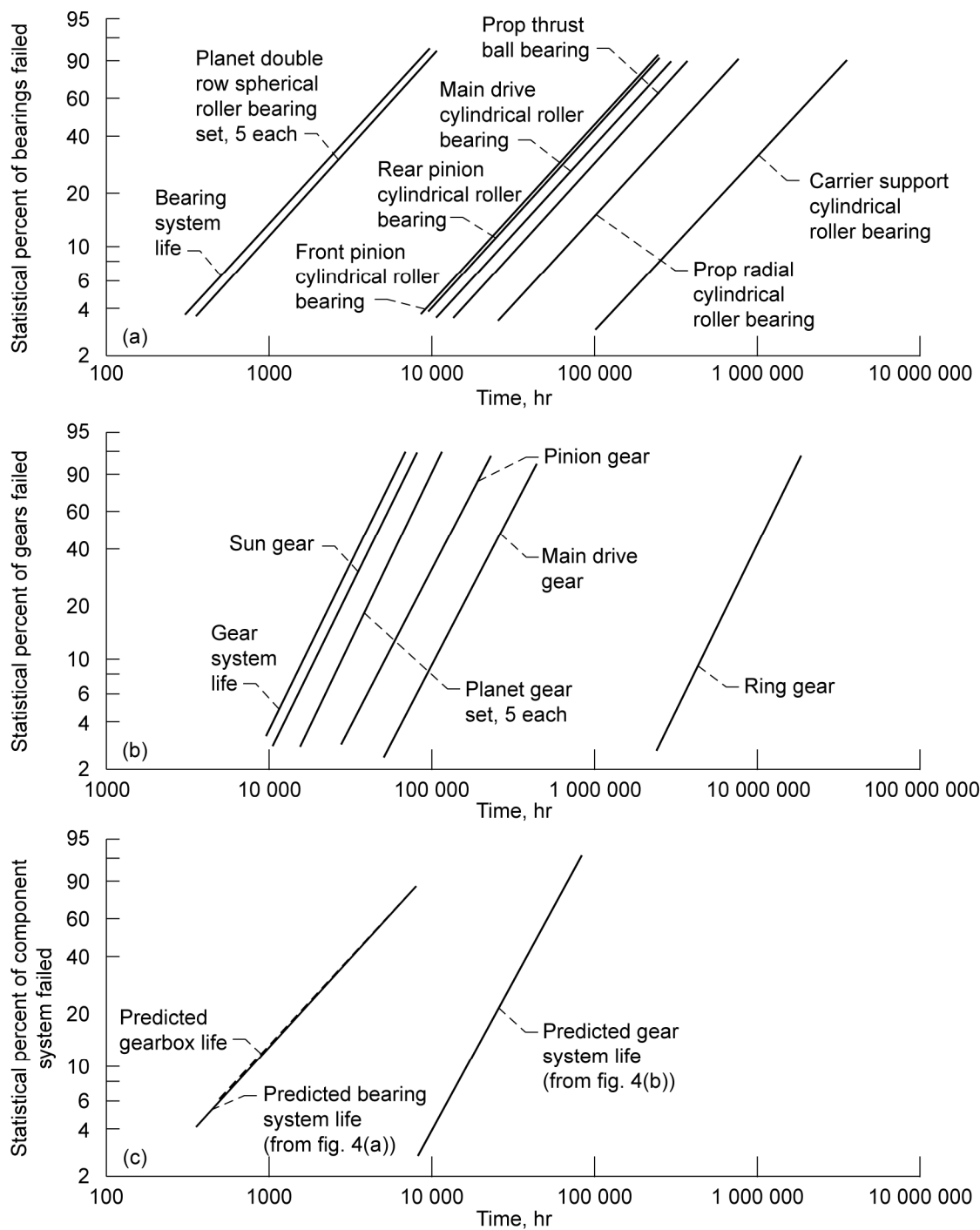


Figure 4.—Predicted lives for commercial turboprop gearbox and its respective bearing and gear components using Lundberg-Palmgren life theory. (a) Bearing component lives. (b) Gear component lives. (c) Gearbox life and component lives.

calculations is dependent on how close the defined mission profile is to actual flight operation.

The gearboxes are condition monitored and are removed from service on the detection of a perceived component failure. At the time of removal, the gearboxes are functional. The removal precludes secondary damage. That is, the damage is limited to the failed component.

Field data were collected for 64 new commercial turboprop gearboxes. From these field data, the resultant time to removal of each gearbox is plotted in the Weibull plot of figure 5. For these data, there was not a breakdown of the cause for removal or the percent of each component that had failed. The resultant L_{10} life from the field data was 5627 hr and the Weibull slope e was 2.189. Using the Lundberg-Palmgren method (above), the predicted L_{10} life was 774 hr and the Weibull slope e was 1.125. The field data suggest that the life of the gearbox was underpredicted by a factor of 7.56.

Although errors in the assumed operating profile of the gearbox may account for the difference between actual and predicted life, it is suggested that using the Lundberg-Palmgren equations results in a life prediction that is too low for the bearings.

Referring to equation (4), in their 1952 publication (ref. 10), Lundberg and Palmgren calculate a load-life exponent p equal to 10/3 for roller bearings, where one raceway has point contact and the other raceway has line contact. The 10/3 load-life exponent has been incorporated in the ANSI/ABMA/ISO standards first published in 1953 (refs. 12 to 14). Their assumption of point and line contact may have been correct for many types of roller bearings then in use. However, it is no longer the case for most roller bearings manufactured today and, most certainly, for cylindrical roller bearings. Experience and the analysis suggest that the 10/3 load-life exponent p for roller bearings is incorrect and underpredicts roller bearing life (ref. 34).

The work of Poplawski, Peters, and Zaretsky (ref. 34) suggests that p for roller bearings is equal to or greater than 4 but is less than 5. This premise can be easily tested based on the data for the turboprop gearbox.

From equation (17) assuming that the bearing system has the same Weibull slope as that of the gearbox (that $e = 2.189$),

$$\frac{1}{L_{sys}^{e_s}} = \frac{1}{L_B^{e_B}} + \frac{1}{L_G^{e_G}} \quad (18a)$$

$$\frac{1}{(5627)^{2.189}} = \frac{1}{L_B^{2.189}} + \frac{1}{(16680)^{2.5}} \quad (18b)$$

From equation (18b), the actual bearing system life is

$$L_B = 5627 \text{ hr} \quad (18c)$$

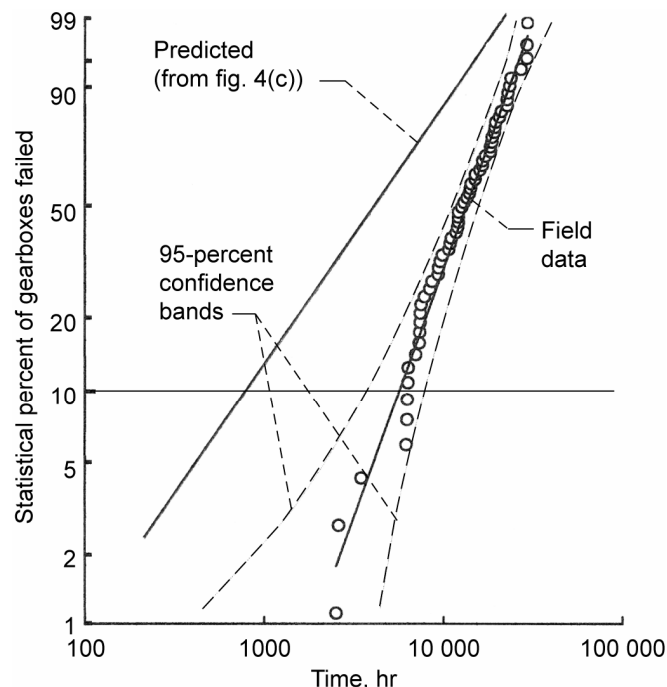


Figure 5.—Field data for lives of turboprop gearboxes compared with predicted lives using Lundberg-Palmgren life theory. Failure index, 59 out of 64.

From Lundberg-Palmgren (ref. 10), the predicted bearing system life is

$$L_B \sim \left(\frac{C_D}{P_{eq}} \right)^{10/3} \sim 774 \text{ hr} \quad (19a)$$

Then,

$$\left(\frac{C_D}{P_{eq}} \right) \sim 7.35 \quad (19b)$$

Calculating a revised value for the load-life exponent p for the gearbox bearings based on the actual bearing system life of 5627 hr (eq. (18c)),

$$\left(\frac{C_D}{P_{eq}} \right)^p \sim (7.35)^p \sim 5627 \text{ hr} \quad (20a)$$

Solving for load-life exponent p ,

$$p = 4.33 \quad (20b)$$

where according to Poplawski, Peters, and Zaretsky (ref. 34),

$$4 \leq p \leq 5 \quad (20c)$$

Were the bearing lives to be recalculated with a load-life exponent p equal to 4.33, the predicted L_{10} life of the gearbox would be equal to the actual life obtained in the field.

Summary of Results

Laboratory fatigue data for rolling-element bearings and gears coupled with probabilistic life prediction and elastohydrodynamic analysis were used to predict the life and reliability of a commercial turboprop gearbox. These data were compared with field data. The following results were obtained.

1. Using Lundberg-Palmgren theory, the predicted gearbox L_{10} life was less than that obtained in the field. The predicted gearbox L_{10} life was 774 hr whereas the actual L_{10} life was 5627 hr.
2. The gearbox life was dependent on the system life of the rolling-element bearings in the gearbox. Changing the load-life exponent p for the bearings from 10/3 to 4.33 would give a predicted gearbox L_{10} life of 5627 hr.
3. The ANSI/ABMA/ISO standards using the unmodified Lundberg-Palmgren theory underpredict rolling-element bearing life resulting in conservative values for the gearbox life prediction.

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REPORT DOCUMENTATION PAGE			Form Approved OMB No. 0704-0188	
Public reporting burden for this collection of information is estimated to average 1 hour per response, including the time for reviewing instructions, searching existing data sources, gathering and maintaining the data needed, and completing and reviewing the collection of information. Send comments regarding this burden estimate or any other aspect of this collection of information, including suggestions for reducing this burden, to Washington Headquarters Services, Directorate for Information Operations and Reports, 1215 Jefferson Davis Highway, Suite 1204, Arlington, VA 22202-4302, and to the Office of Management and Budget, Paperwork Reduction Project (0704-0188), Washington, DC 20503.				
1. AGENCY USE ONLY (Leave blank)	2. REPORT DATE January 2007	3. REPORT TYPE AND DATES COVERED Technical Memorandum		
4. TITLE AND SUBTITLE Design of Oil-Lubricated Machine for Life and Reliability		5. FUNDING NUMBERS WBS 561581.02.07.03.03.01		
6. AUTHOR(S) Erwin V. Zaretsky				
7. PERFORMING ORGANIZATION NAME(S) AND ADDRESS(ES) National Aeronautics and Space Administration John H. Glenn Research Center at Lewis Field Cleveland, Ohio 44135-3191		8. PERFORMING ORGANIZATION REPORT NUMBER E-15577		
9. SPONSORING/MONITORING AGENCY NAME(S) AND ADDRESS(ES) National Aeronautics and Space Administration Washington, DC 20546-0001		10. SPONSORING/MONITORING AGENCY REPORT NUMBER NASA TM-2007-214362		
11. SUPPLEMENTARY NOTES Prepared for the Seventh International Symposia on Tribology (INSYCONT 2006) cosponsored by the AGH University of Science and Technology, the Polish Academy of Science, the Institute for Terotechnology, and the Polish Tribology Society, Cracow, Poland, September 14-16, 2006. Responsible person, Erwin V. Zaretsky, organization code RX, 216-433-3241.				
12a. DISTRIBUTION/AVAILABILITY STATEMENT Unclassified - Unlimited Subject Categories: 01, 05, 37, and 39 Available electronically at http://gltrs.grc.nasa.gov This publication is available from the NASA Center for AeroSpace Information, 301-621-0390.		12b. DISTRIBUTION CODE		
13. ABSTRACT (Maximum 200 words) In the post-World War II era, the major technology drivers for improving the life, reliability, and performance of rolling-element bearings and gears have been the jet engine and the helicopter. By the late 1950s, most of the materials used for bearings and gears in the aerospace industry had been introduced into use. By the early 1960s, the life of most steels was increased over that experienced in the early 1940s, primarily by the introduction of vacuum degassing and vacuum melting processes in the late 1950s. The development of elastohydrodynamic (EHD) theory showed that most rolling bearings and gears have a thin film separating the contacting bodies during motion and it is that film which affects their lives. Computer programs modeling bearing and gear dynamics that incorporate probabilistic life prediction methods and EHD theory enable optimization of rotating machinery based on life and reliability. With improved manufacturing and processing, the potential improvement in bearing and gear life can be as much as 80 times that attainable in the early 1950s. The work presented summarizes the use of laboratory fatigue data for bearings and gears coupled with probabilistic life prediction and EHD theories to predict the life and reliability of a commercial turboprop gearbox. The resulting predictions are compared with field data.				
14. SUBJECT TERMS Lubrication; Reliability; Life prediction; Rolling bearings; Bearings; Gears; Gearbox; Probabilistic life prediction; Rolling-element bearings; Turboprop gearbox; Elastohydrodynamic lubrication			15. NUMBER OF PAGES 16	
			16. PRICE CODE	
17. SECURITY CLASSIFICATION OF REPORT Unclassified	18. SECURITY CLASSIFICATION OF THIS PAGE Unclassified	19. SECURITY CLASSIFICATION OF ABSTRACT Unclassified	20. LIMITATION OF ABSTRACT	

